

### Part Chapter 2: Cameras "Lenses"

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### Pinhole size / aperture

How does the size of the aperture affect the image we'd get?



Fig. 5.96 The pinhole camera. Note the variation in image clarity as the hole diameter decreases. [Photos courtesy Dr. N. Joel, UNESCO.]



### Pinhole vs. lens





# Adding a lens



A lens focuses light onto the film

- Rays passing through the center are not deviated
- All parallel rays converge to one point on a plane located at the *focal length f*



### **Cameras with lenses**



- A lens focuses parallel rays onto a single focal point
- Gather more light, while keeping focus; make pinhole perspective projection practical





Snell's law

 $n_1 \sin \alpha_1 = n_2 \sin \alpha_2$ 

![](_page_5_Figure_4.jpeg)

![](_page_6_Figure_0.jpeg)

![](_page_7_Figure_0.jpeg)

![](_page_7_Figure_1.jpeg)

#### Thin Lenses

spherical lens surfaces; thickness << radii; same refractive index on both sides; all rays emerging from P and passing through the lens are focused at P'. Let  $n_1=1$  (vaccuum) and  $n_2=n$ .

![](_page_7_Figure_4.jpeg)

![](_page_8_Figure_0.jpeg)

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spherical lens surfaces; thickness << radii; same refractive index on both sides; all rays emerging from P and passing through the lens are focused at P'. Let  $n_1=1$  (vaccuum) and  $n_2=n$ .

![](_page_8_Figure_3.jpeg)

$$\begin{cases} x' = z' \frac{x}{z} \\ y' = z' \frac{y}{z} \end{cases}$$

where 
$$\frac{1}{z'} - \frac{1}{z} = \frac{1}{f}$$
 and  $f$ 

http://www.phy.ntnu.edu.tw/java/Lens/lens\_e.html

 $=\frac{R}{2(n-1)}$ 

![](_page_9_Picture_0.jpeg)

#### Thick Lens

![](_page_9_Figure_2.jpeg)

### Focus and depth of field

![](_page_10_Picture_1.jpeg)

![](_page_10_Picture_2.jpeg)

Image credit: cambridgeincolour.com

![](_page_11_Picture_0.jpeg)

### The depth-of-field

![](_page_11_Figure_2.jpeg)

![](_page_12_Picture_0.jpeg)

# Focus and depth of field

# Depth of field: distance between image planes where blur is tolerable

![](_page_12_Figure_3.jpeg)

Thin lens: scene points at distinct depths come in focus at different image planes.

(Real camera lens systems have greater depth of field.)

—— "circles of confusion" ——

Shapiro and Stockman

![](_page_13_Picture_0.jpeg)

# Focus and depth of field

w does the aperture affect the depth of field?

![](_page_13_Picture_3.jpeg)

• A smaller aperture increases the range in which the object is approximately in focus

Flower images from Wikipedia <u>http://en.wikipedia.org/wiki/Depth\_of\_field</u>

Slide from S. Seitz

![](_page_14_Picture_0.jpeg)

### The depth-of-field

![](_page_14_Figure_2.jpeg)

![](_page_15_Picture_0.jpeg)

#### The depth-of-field

![](_page_15_Figure_2.jpeg)

decreases with d+, increases with Z<sub>0</sub>+ strike a balance between incoming light and sharp depth range

![](_page_16_Picture_0.jpeg)

#### Deviations from the lens model

- 3 assumptions :
- 1. all rays from a point are focused onto 1 image point
- 2. all image points in a single plane
- 3. magnification is constant
- deviations from this ideal are *aberrations*

![](_page_17_Picture_0.jpeg)

#### Aberrations

2 types :

1. geometrical

2. chromatic

geometrical : small for paraxial rays study through 3<sup>rd</sup> order optics  $sin(\theta) \approx \theta - \frac{\theta^3}{6}$ 

*chromatic :* refractive index function of wavelength

![](_page_18_Picture_0.jpeg)

#### **Geometrical aberrations**

spherical aberration

astigmatism

distortion

🖵 coma

aberrations are reduced by combining lenses

![](_page_18_Figure_7.jpeg)

![](_page_19_Picture_0.jpeg)

#### Spherical aberration

rays parallel to the axis do not converge

outer portions of the lens yield smaller focal lenghts

![](_page_19_Figure_4.jpeg)

![](_page_20_Picture_0.jpeg)

# Astigmatism

Different focal length for inclined rays

![](_page_20_Figure_3.jpeg)

![](_page_21_Picture_0.jpeg)

pincushion (tele-photo)

barrel (wide-angle)

### Distortion

magnification/focal length different for different angles of inclination

![](_page_21_Picture_3.jpeg)

Can be corrected! (if parameters are know)

![](_page_22_Picture_0.jpeg)

### Coma

point off the axis depicted as comet shaped blob

![](_page_22_Picture_3.jpeg)

![](_page_23_Picture_0.jpeg)

#### **Chromatic aberration**

# rays of different wavelengths focused in different planes

![](_page_23_Figure_3.jpeg)

![](_page_23_Figure_4.jpeg)

![](_page_23_Picture_5.jpeg)

The image is blurred and appears colored at the fringe.

cannot be removed completely

sometimes achromatization is achieved for

more than 2 wavelengths

![](_page_23_Picture_10.jpeg)

![](_page_24_Picture_0.jpeg)

### Lens materials

reference wavelengths :

 $\lambda_F = 486.13nm$   $\lambda_d = 587.56nm$  $\lambda_C = 656.28nm$ 

lens characteristics :

1. refractive index  $n_d$ 2. Abbe number  $V_d = (n_d - 1) / (n_F - n_C)$ 

typically, both should be high allows small components with sufficient refraction

notation : e.g. glass BK7(517642)  $n_d = 1.517$  and  $V_d = 64.2$ 

![](_page_25_Picture_0.jpeg)

#### Lens materials

![](_page_25_Figure_2.jpeg)

#### additional considerations :

humidity and temperature resistance, weight, price,...

![](_page_26_Picture_0.jpeg)

### Vignetting

![](_page_26_Figure_2.jpeg)

![](_page_26_Picture_3.jpeg)

![](_page_26_Picture_4.jpeg)