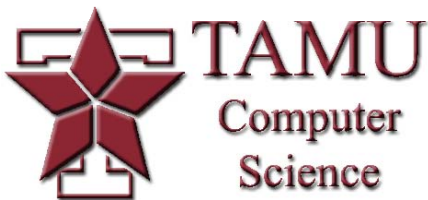


# CSCE 641 Computer Graphics: Image Mosaicing

Jinxiang Chai



*Source:*

[faculty.cs.tamu.edu/jchai/cpsc641\\_spring10/lectures/lecture8.ppt](http://faculty.cs.tamu.edu/jchai/cpsc641_spring10/lectures/lecture8.ppt)

# Outline

Image registration

- How to break assumptions?

3D-2D registration

Image mosaicing

# Mosaics: Stitching Image Together



virtual wide-angle camera

# Mosaic Procedure

Basic Procedure

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- Take a sequence of images from the same position
  - Rotate the camera about its optical center

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  - Rotate the camera about its optical center
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- Transform the second image to overlap with the first
- Blend the two together to create a mosaic



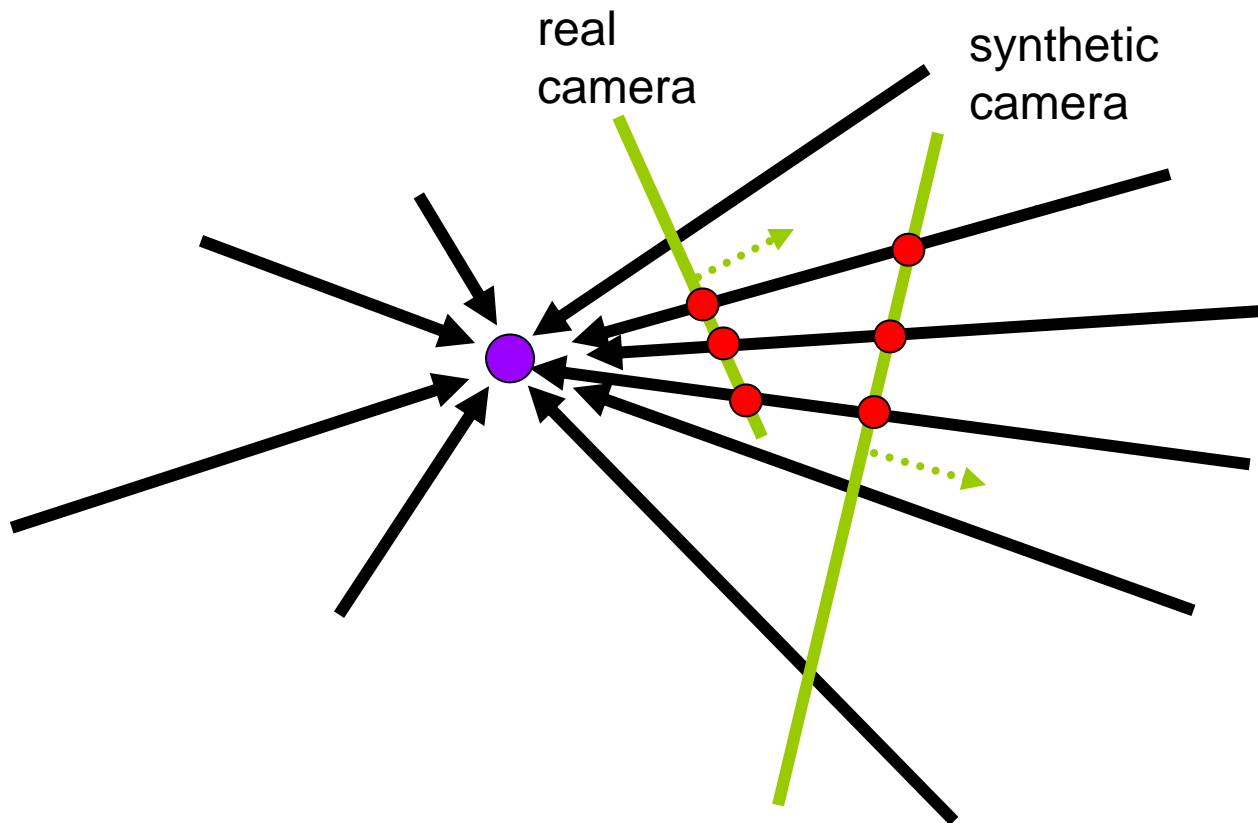
# Mosaic Procedure

## Basic Procedure

- Take a sequence of images from the same position
  - Rotate the camera about its optical center
- Compute transformation between second image and first
- Transform the second image to overlap with the first
- Blend the two together to create a mosaic
- If there are more images, repeat

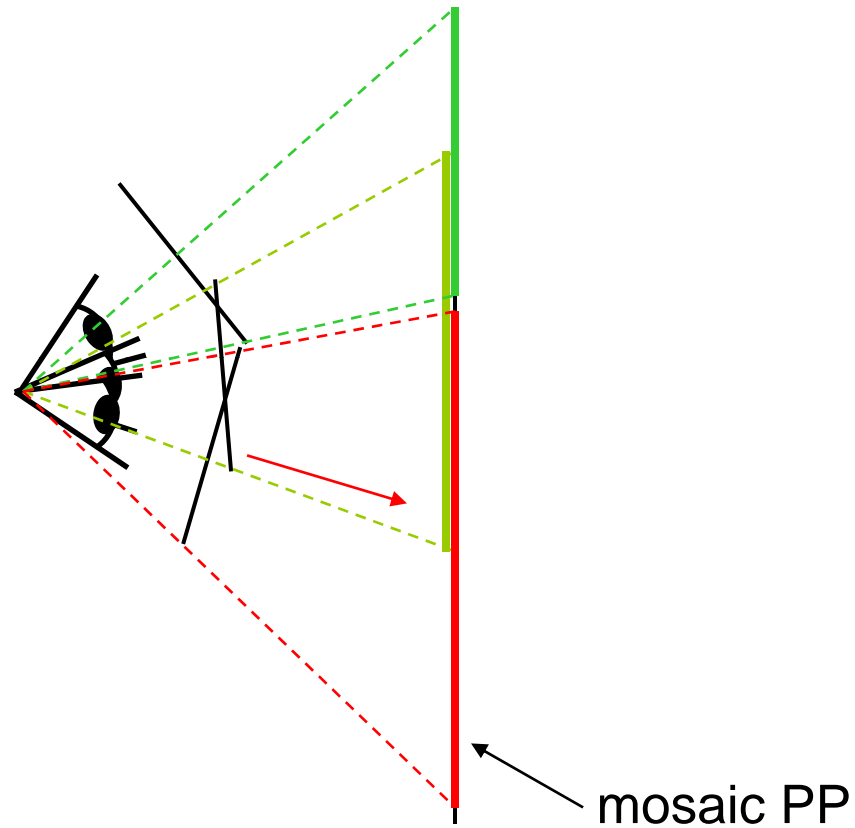
# Image Mosaic

Is a pencil of rays contains all views



Can generate any synthetic camera view as long as it has **the same center of projection!**

# Image Re-projection



The mosaic has a natural interpretation in 3D

- The images are reprojected onto a common plane
- The mosaic is formed on this plane
- Mosaic is a *synthetic wide-angle camera*

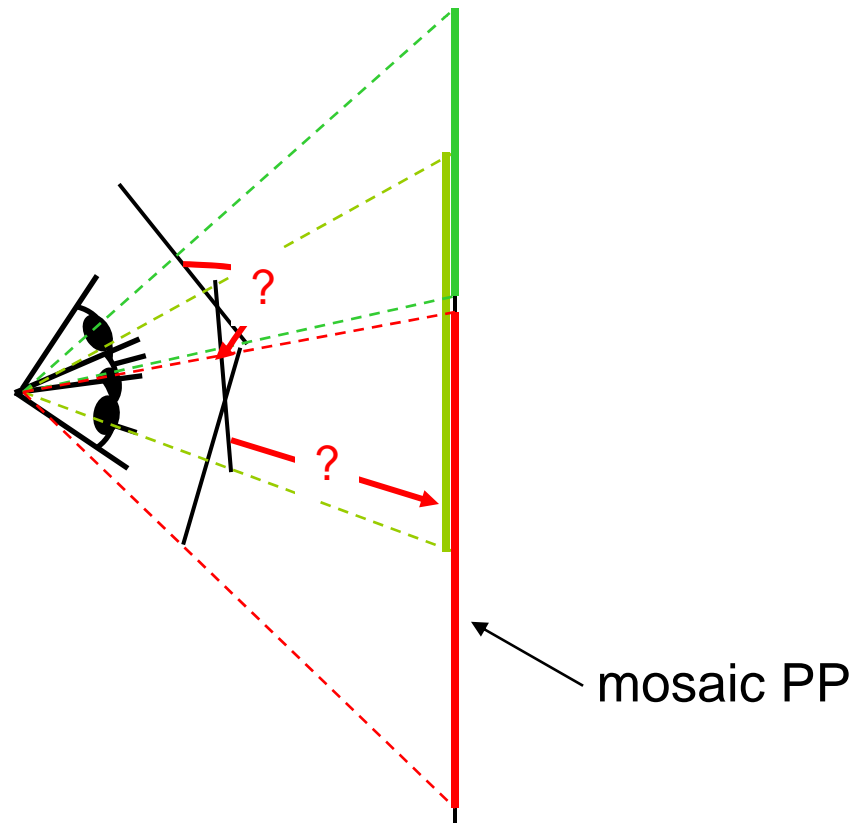
# Issues in Image Mosaic

How to relate two images from the same camera center?

- image registration

How to re-project images to a common plane?

- image warping



# Image Mosaicing

Geometric relationship between images

# Image Mosaicing

## Geometric relationship between images

- Use 8-parameter projective transformation matrix

$$\begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix} = \begin{vmatrix} a & b & c \\ d & e & f \\ g & h & 1 \end{vmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$$

# Image Mosaicing

## Geometric relationship between images

- Use 8-parameter projective transformation matrix

$$\begin{pmatrix} x' \\ y' \\ 1 \end{pmatrix} = \begin{vmatrix} a & b & c \\ d & e & f \\ g & h & 1 \end{vmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$$

- Use a 3D rotation model (one R per image)

$$\begin{vmatrix} r_{00} & r_{01} & f_0 r_{02} \\ r_{10} & r_{11} & f_0 r_{12} \\ r_{20}/f_1 & r_{21}/f_1 & f_0 r_{21}/f_1 \end{vmatrix}$$

Derive it by yourself!

# Image Mosaicing

## Geometric relationship between images

- Use 8-parameter projective transformation matrix
- Use a 3D rotation model (one R per image)

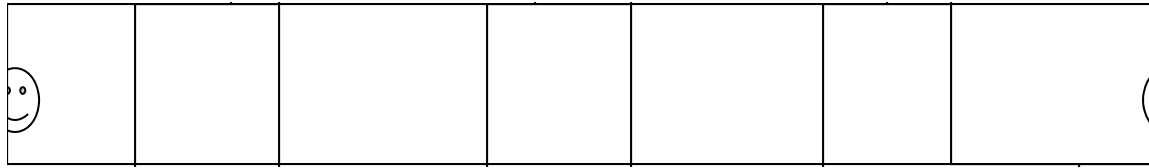
## Register *all* pairwise overlapping images

- Feature-based registration
- Pixel-based registration

*Chain* together inter-frame rotations



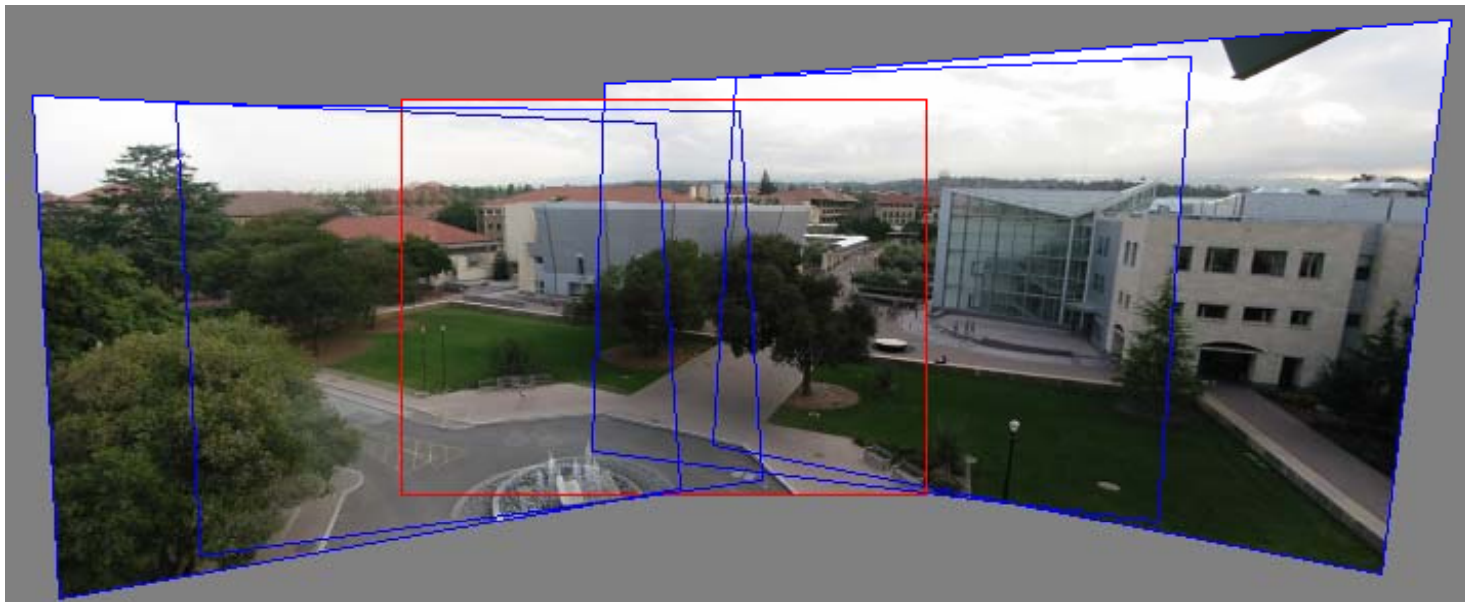
# Image Stitching



Stitch pairs together, blend, then crop

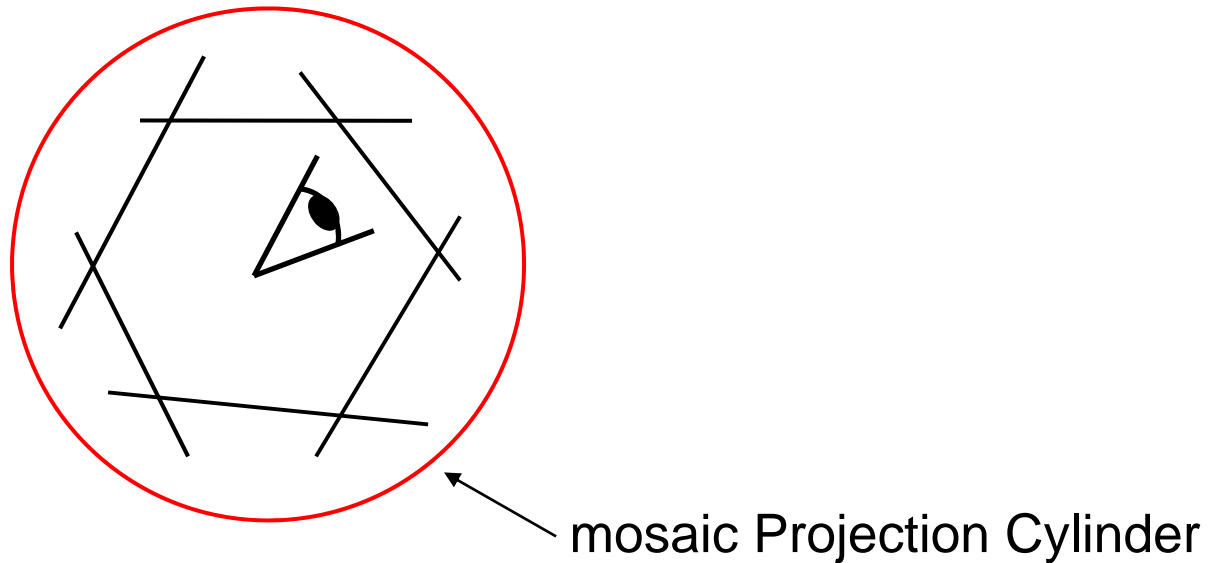
# Image Stitching

A big image stitched from 5 small images

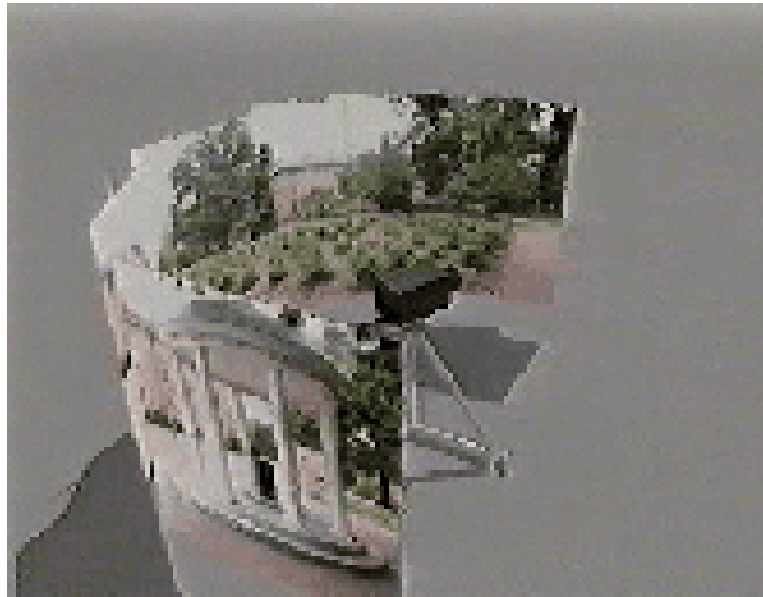


# Panoramas

What if you want a 360° field of view?



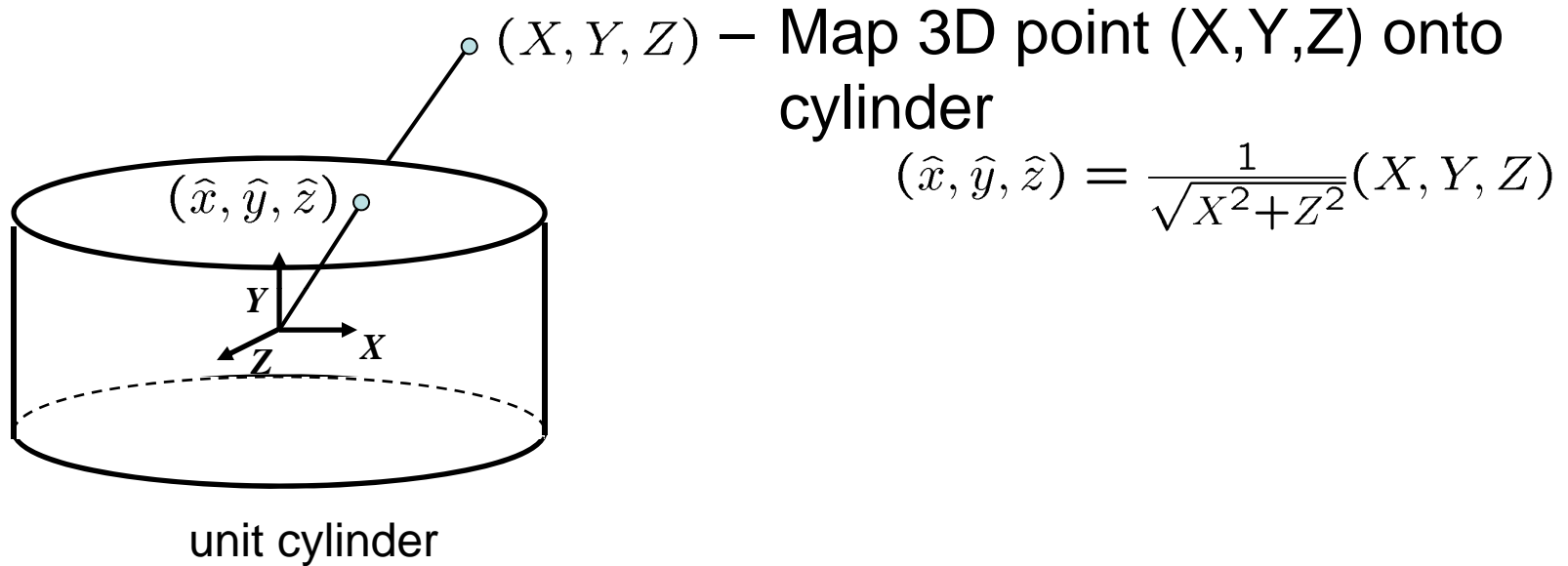
# Cylindrical Panoramas



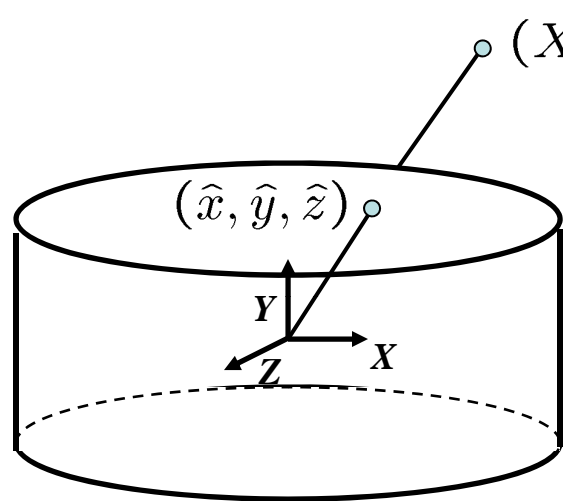
## Steps

- Re-project each image onto a cylinder
- Blend
- Output the resulting mosaic

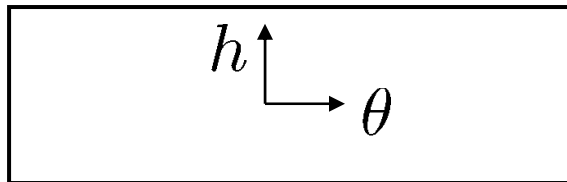
# Cylindrical Projection



# Cylindrical Projection



unit cylinder



unwrapped cylinder

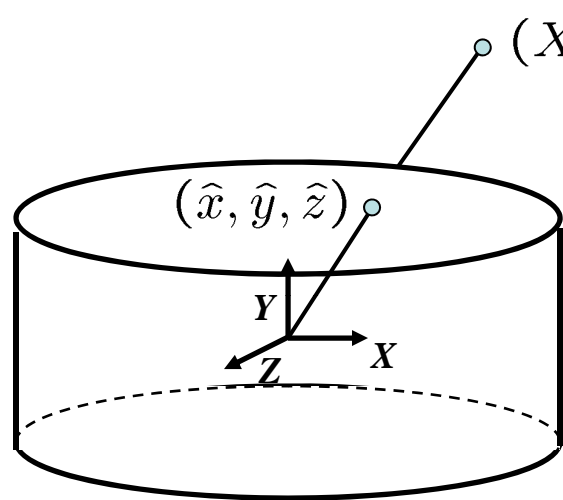
$(X, Y, Z)$  – Map 3D point  $(X, Y, Z)$  onto cylinder

$$(\hat{x}, \hat{y}, \hat{z}) = \frac{1}{\sqrt{X^2 + Z^2}}(X, Y, Z)$$

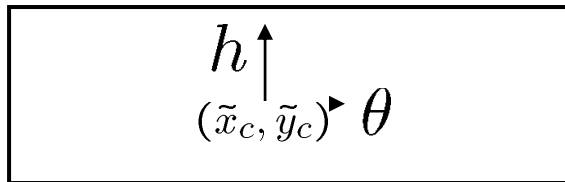
– Convert to cylindrical coordinates

$$(\sin\theta, h, \cos\theta) = (\hat{x}, \hat{y}, \hat{z})$$

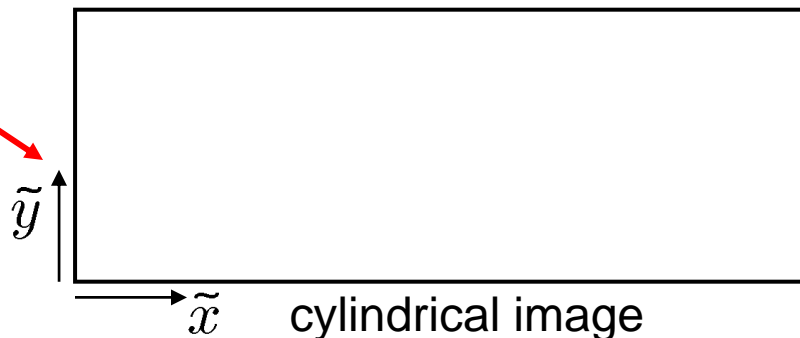
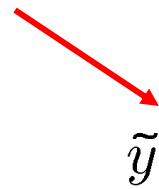
# Cylindrical Projection



unit cylinder



unwrapped cylinder



cylindrical image

$(X, Y, Z)$  – Map 3D point  $(X, Y, Z)$  onto cylinder

$$(\hat{x}, \hat{y}, \hat{z}) = \frac{1}{\sqrt{X^2 + Z^2}}(X, Y, Z)$$

– Convert to cylindrical coordinates

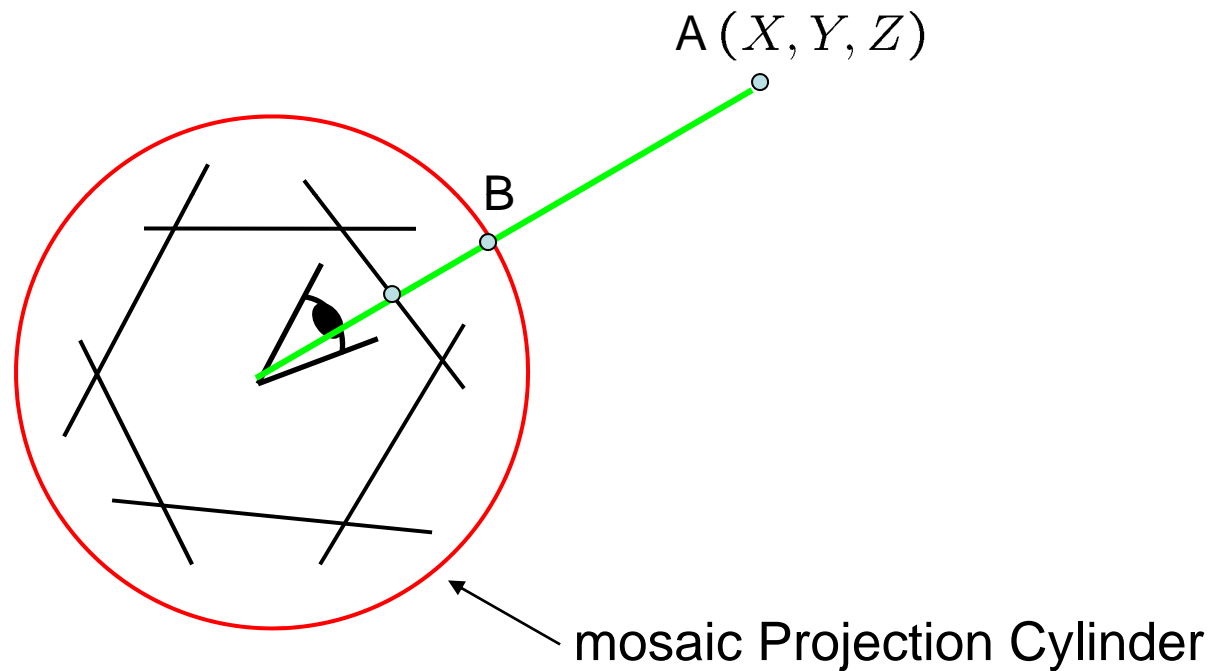
$$(\sin\theta, h, \cos\theta) = (\hat{x}, \hat{y}, \hat{z})$$

– Convert to cylindrical image coordinates

$$(\tilde{x}, \tilde{y}) = (s\theta, sh) + (\tilde{x}_c, \tilde{y}_c)$$

- $s$  defines size of the final image

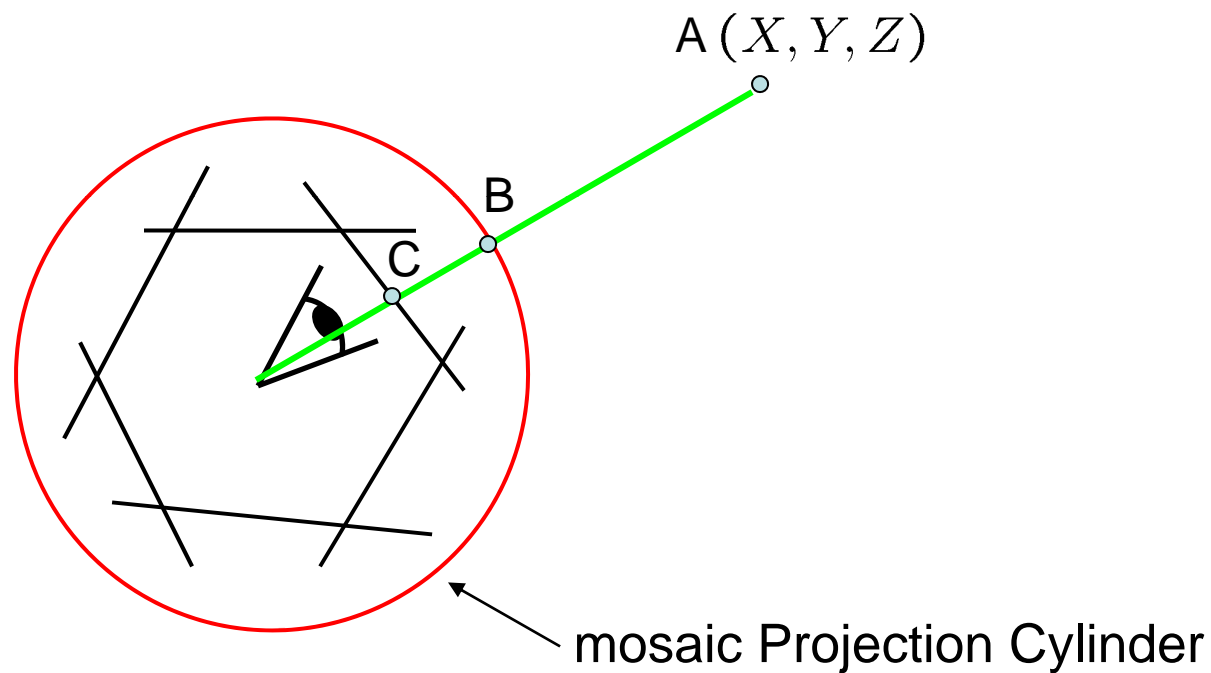
# Cylindrical Panoramas



Cannot map point A to Point B without knowing (X,Y,Z)



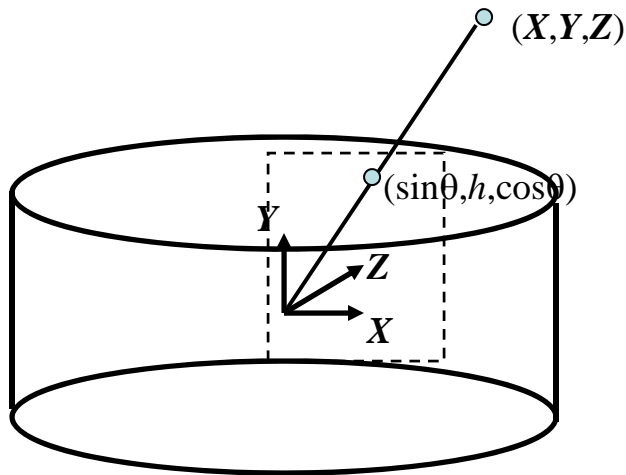
# Cylindrical Panoramas



But we can map point C (images) to Point B.

# Cylindrical Warping

Given focal length  $f$   
and image center  
 $(x_c, y_c)$



$$\theta = (x_{cyl} - x_c) / f$$

$$h = (y_{cyl} - y_c) / f$$

$$\hat{x} = \sin \theta$$

$$\hat{y} = h$$

$$\hat{z} = \cos \theta$$

$$x = f \hat{x} / \hat{z} + x_c$$

$$y = f \hat{y} / \hat{z} + y_c$$

# Cylindrical Panoramas

Map image to cylindrical or spherical coordinates  
– need *known* focal length



**Image 384x300**



**f = 180 (pixels)**

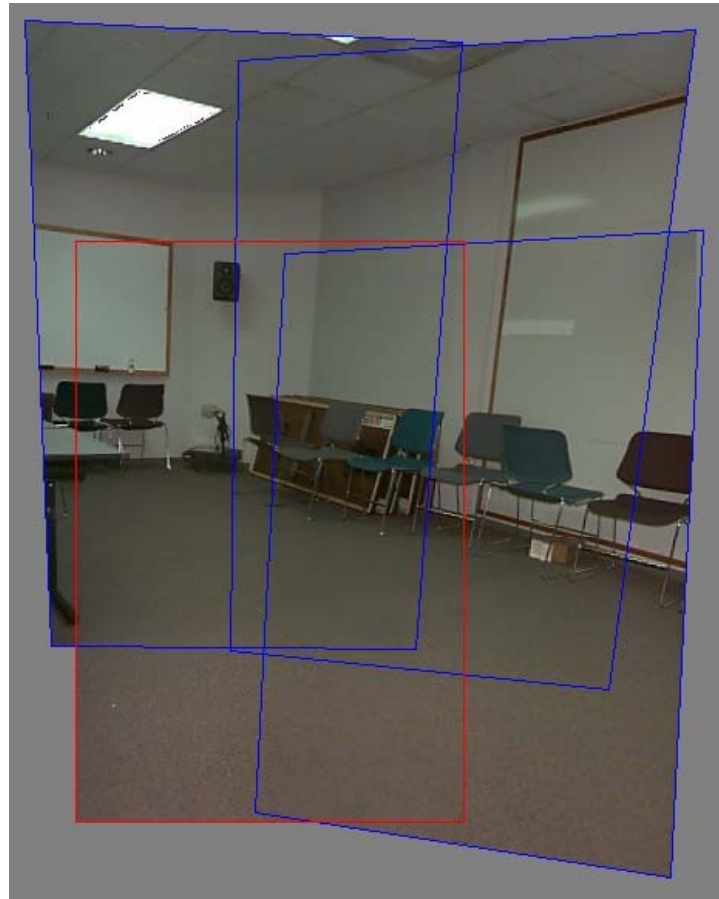


**f = 280**



**f = 380**

# Cylindrical Panorama



3D rotation registration of four images taken with a handheld camera.

# Cylindrical Panorama



# Recognizing panoramas

- A fully automatic 2D image stitcher system



Input Images



Output panorama #1

# Recognizing panoramas

- A fully automatic 2D image stitcher system



Input Images



Output panorama #2

# Recognizing panoramas

- A fully automatic 2D image stitcher system



Input Images



Output panorama #3



# Recognizing panoramas

- A fully automatic 2D image stitcher system



Input Images

- How to recognize which images can be used for panoramas?
- How to stitch them automatically?

# Recognizing panoramas

- A fully automatic 2D image stitcher system



# Recognizing panoramas

- A fully automatic 2D image stitcher system



- Image matching with [SIFT](#) features
- For every image, find the M best images with RANSAC
- Form a graph and find connected component in the graph
- Stitching and blending.

# Outline

Image registration

- How to break assumptions? (cont.)

3D-2D registration

Image mosaicing